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Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

# GCSE MATHEMATICS

H

**Higher Tier** 

Paper 3 Calculator

Tuesday 11 June 2019

Morning

Time allowed: 1 hour 30 minutes

## **Materials**

For this paper you must have:

- a calculator
- · mathematical instruments.



#### Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

#### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

#### **Advice**

In all calculations, show clearly how you work out your answer.



For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26–27	
TOTAL	

# Answer all questions in the spaces provided

Work out £1.50 as a fraction of 60p Circle your answer.

[1 mark]

 $\frac{2}{5}$ 

 $\frac{1}{4}$ 

 $\frac{4}{1}$ 

 $\frac{5}{2}$ 

2 For a biased dice,  $P(6) = \frac{3}{5}$ 

Circle the probability of two sixes when the dice is rolled twice.

[1 mark]

 $\frac{6}{25}$ 

 $\frac{6}{10}$ 

 $\frac{9}{25}$ 

 $\frac{9}{5}$ 

3 Circle the lowest common multiple (LCM) of 5, 15 and 25

[1 mark]

5

45

75

150

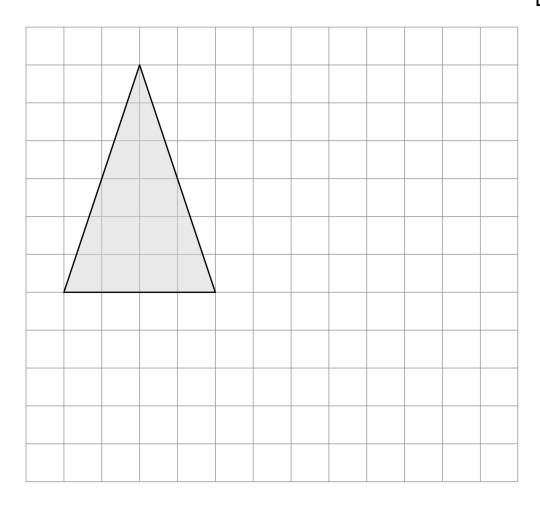
4 Circle the **two** roots of (x-5)(x+3) = 0

[1 mark]

- **-**5
- -3
- 3
- 5

On the grid, draw an enlargement of the triangle with scale factor  $\frac{1}{2}$ 

[2 marks]



6

To the nearest pound, Jon has £9  To the nearest 50p, Ellie has £6.50	
Work out the maximum possible total amount of money.	[3 marks
Answer £	



7 Two solids, J and K, have the same density.

Complete the table.

Include units in your answers.

[3 marks]

	J	К
Mass	48 g	78 g
Volume	8 cm <sup>3</sup>	
Density		

8 Rearrange y = 3x - 2 to make x the subject.

Circle your answer.

[1 mark]

$$x = \frac{y}{3} - 2$$

$$x = \frac{y+2}{3}$$

$$x = \frac{y - 2}{3}$$

$$x = \frac{y}{3} - 2$$
  $x = \frac{y+2}{3}$   $x = \frac{y-2}{3}$   $x = \frac{y}{3} + 2$ 

9	Towns <i>P</i> , <i>Q</i> and <i>R</i> are connected by roads <i>PQ</i> , <i>PR</i> and <i>QR</i> .		
	PR is 10 km longer than PQ.		
	QR is twice as long as PR.		
	The total length of the three roads is 170 km		
		Not drawn	
	R	accurately	
	P		
	Q		
	<b>Q</b>		
	Work out the length of <i>PQ</i> .		
	Work out the length of 7 Q.		[4 marks]
	Anguar	lem	
	Answer	km	



Mia wants to borrow £6000 and repay it, with interest, after two years.

She sees two offers for loans.

## Offer 1

Compound interest 3% per year

## Offer 2

Compound interest First year 1% Second year 5%

Mia says,

"I will pay back the same amount because the average of 1% and 5% is 3%"

Is she correct?

You <b>must</b> show your working.	[3 marks]

Turn over for the next question

7





11	Here are two se	ts of numbe	ers, A and B.				
		Set A	<b>\</b>		Set B		
		200 104	160 100	270 30	400 0 <i>x</i>	483	
	mean of Set A:	mean of Se	et B = 3 : 8				
	Work out the va	lue of x.					[4 marks]
		Answer _					



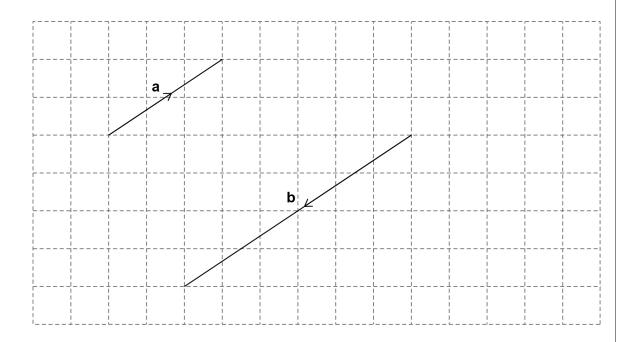
A straight line	
has gradient 4	
and	
passes through the point (5, 23)	
Work out the equation of the line.	
Give your answer in the form $y = mx + c$	[3 marks
	Įo marko
Answer	_

Turn over for the next question

7



13 (a) Vectors **a** and **b** are drawn on a grid.



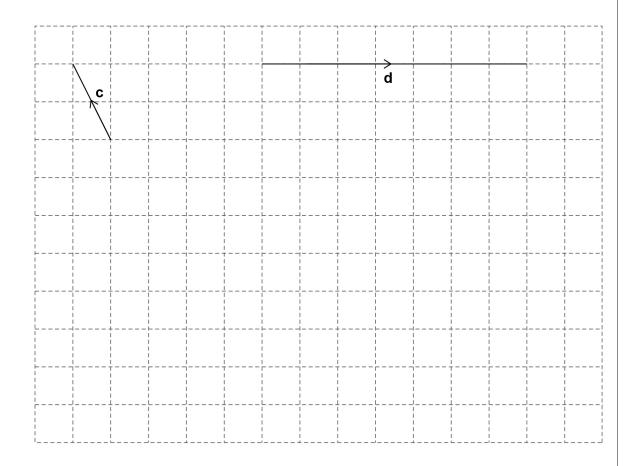
Write **b** in terms of **a**.

[1 mark]

b =



13 (b) Vectors **c** and **d** are drawn on a grid.



On the grid above, draw a vector representing  $\mathbf{c} - \mathbf{d}$ 

[2 marks]

Turn over for the next question

3



14		number of boys : number of girls = 7 : 8 number of boys : number of girls = 3 : 4	
	Which statemen Tick <b>one</b> box.	t must be true?	[1 mark]
		Class X has more boys than class Y	[
		Class X has twice as many girls as class Y	
		Class X has a greater proportion of boys than class Y	
		Class X has the same proportion of boys as class Y	
15	Simplify fully	$\frac{a^3b^2}{cd} \times \frac{c}{ab^5}$	[3 marks]
		Answer	







17 A factory makes kettle
---------------------------

Four samples of kettles are tested for faults.

Each sample has size 200

Here are the relative frequencies of faulty kettles in the samples.

Sample	Р	Q	R	S
Relative frequency	0.03	0.035	0.015	0.01

Work out the range of the number of faulty kettles in the four samples.	[3 marks]	
Answer		



18 (a)	Write $x(3x-9) = 4$ in the form $ax^2 + bx + c = 0$ where $a$ , $b$ and	c are integers.
		[1 mark]
	Answer	_
8 (b)	Solve $x(3x - 9) = 4$	
	Give your answers to 2 decimal places.	[2 marks
	Answer	
	Turn over for the next question	

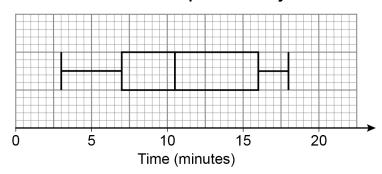


19 Here is some information about the times people took to complete a survey.

Fastest time 3 minutes
Slowest time 18 minutes
Median 11 minutes
Lower quartile 7 minutes
Interquartile range 8 minutes

Ben draws this box plot to show the information.

## Time to complete a survey



Make two criticisms of his box plot.

Criticism 1

[2	m	ar	ks

Criticism 2			



17		
d is directly proportional to the square of $v$ . $d = 6  when  v = 20$		Do no outsid b
Work out an equation connecting $d$ and $v$ .	[3 marks]	
Answer		
Work out the value of $d$ when $v = 30$	[2 marks]	
Answer		
Turn over for the next question		
	d is directly proportional to the square of $v$ . $d$ = 6 when $v$ = 20  Work out an equation connecting $d$ and $v$ .  Answer  Work out the value of $d$ when $v$ = 30  Answer	d is directly proportional to the square of $v$ . $d=6$ when $v=20$ Work out an equation connecting $d$ and $v$ .  [3 marks]  Answer  Work out the value of $d$ when $v=30$ [2 marks]  Answer



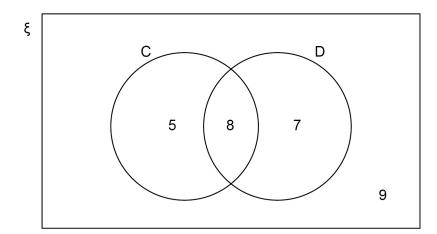
1	Hanif makes green paint by mixing blue paint and yellow paint in the ratio blue : yellow = 7 : 3	
	He buys blue paint in 50-litre containers, each costing £225 He buys yellow paint in 20-litre containers, each costing £80	
	He wants to sell the green paint in 5-litre tins make 40% profit on each tin.	
	How much should he sell each tin for?	[5 marks]
	Answer £	



22  $\xi$  = 29 students in a class

C = students who own a cat

D = students who own a dog



**22** (a) A student is chosen at random.

Circle the probability that the student owns a cat or a dog but not both.

[1 mark]

$$\frac{12}{29}$$

$$\frac{13}{29}$$

$$\frac{15}{29}$$

$$\frac{20}{29}$$

22 (b) A student who owns a dog is chosen at random.

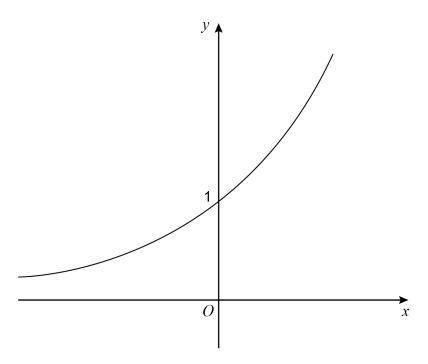
Circle the probability that the student also owns a cat.

[1 mark]

$$\frac{7}{15}$$

$$\frac{8}{15}$$

Here is a sketch of the curve  $y = 2^x$ 



On the axes above, sketch the curve  $y = 3^x$ 

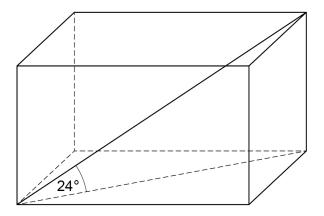
[2 marks]

The length of a diagonal of a cuboid is 20 cm

The diagonal makes an angle of 24° with the base.

Answer \_

The area of the base is 150  $\mathrm{cm}^2$ 



Work out the volume of the cuboid.

[3 marks]

5

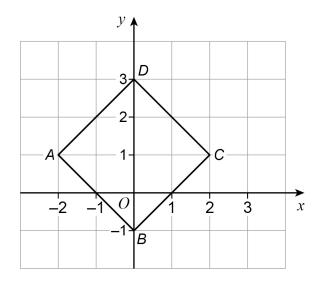
Turn over ▶

 $cm^3$ 



25 ABCD is a square.

A is (-2, 1) B is (0, -1) C is (2, 1) D is (0, 3)



25 (a) A single transformation of ABCD is such that

 $\boldsymbol{B}$  is mapped to  $\boldsymbol{D}$ 

D is mapped to B

A and C are invariant points.

Describe fully the transformation.

[2 marks]

25	(h)	A different <b>single</b> transformation of <i>ABCD</i> is such that
23	( <i>D)</i>	A difficient <b>single</b> transformation of ADOD is such that

B is mapped to D

D is mapped to B

the only invariant point is (0, 1)

Describe fully the transformation.

[3	marks]
----	--------

26	g(x) = 16 - x	$h(x) = x^3$
	g(x) = 10 - x	$\Pi(x) = x$

Solve 
$$gh(x) = 24$$

[3 marks]

*x* = \_\_\_\_\_

Turn over for the next question

8

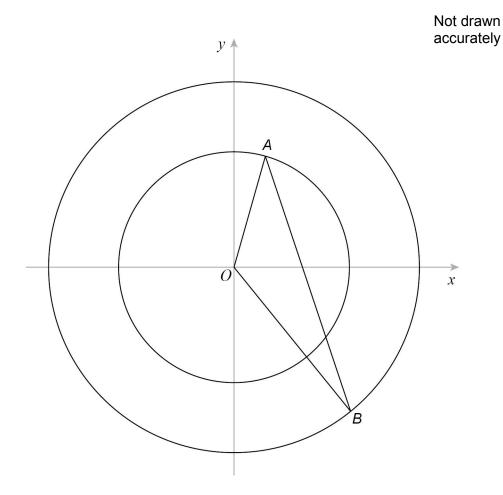


27 In this question, all lengths are in centimetres.

A is a point on a circle, centre O.

 ${\it B}$  is a point on a different circle, centre  ${\it O}$ .

AB = 20



The equation of the larger circle is  $x^2 + y^2 = 144$ 

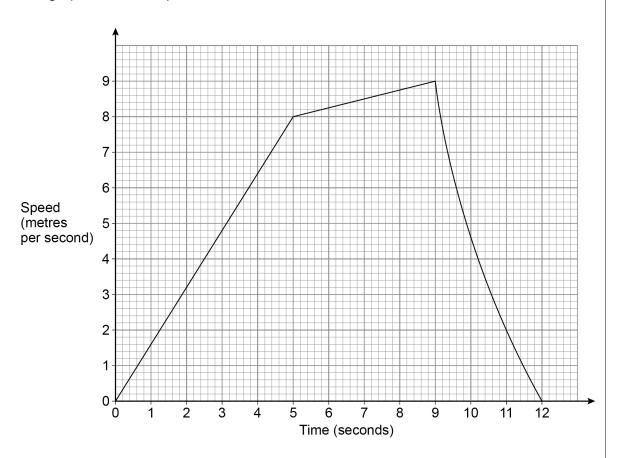
radius of smaller circle : radius of larger circle = 4 : 5

Answer degrees	
Turn over for the next question	



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28	100	runc	for 1	12 cac	conds.
20	ᆫᄄ	าเนแธ	וטו ו	ことってい	JUHUS.

The graph shows his speed.



28	(2)	Show that the	distance he run	e ie lace than	67 5 metres
/n	(a)	Show mai me	distance he min	וגווו צציםו צו צ	in/amenes

[4 marks]	



28	(b)	Work out his average acceleration for the first 9 seconds.		Do not write outside the box
		State the units of your answer.	[2 marks]	
		Answer		
		END OF QUESTIONS		



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